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# Jet and Rocket Propulsion

## AE4451

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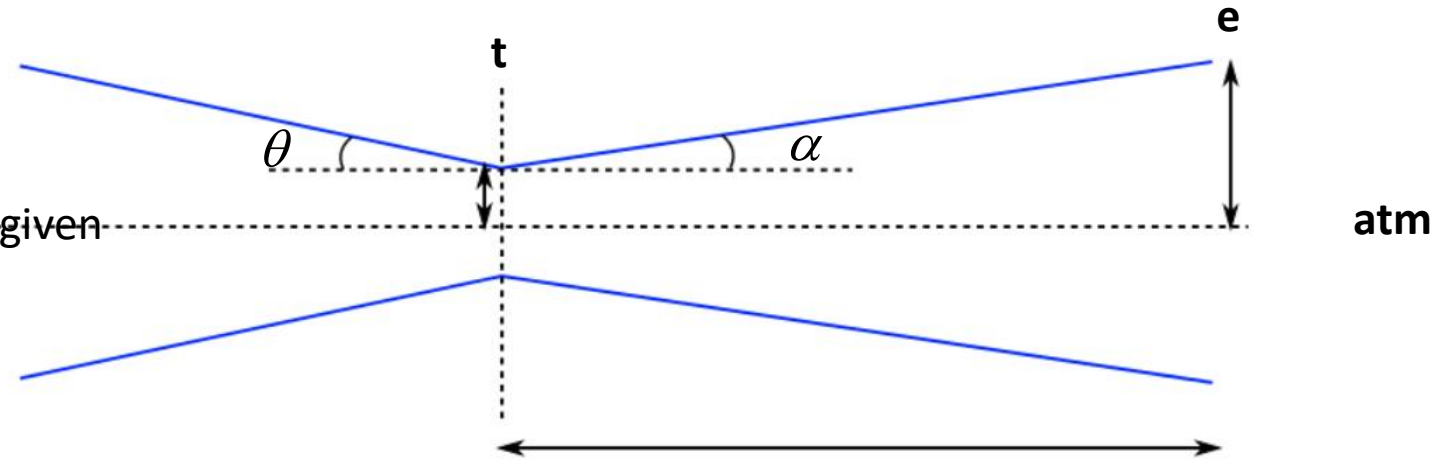
### LECTURE 34

- what we saw in Lecture 33
  - analysis of turbine engine components
    - nozzles and thrust reversers:
      - nozzle types and basic structure (fixed, variable geometry)
      - nozzle coefficients
      - nozzle mixing, thrust vectoring, thrust reversal
- today
  - quick example of nozzle analysis
  - combustors

# Nozzles

## Example

- how can we dimension a nozzle?
- assuming simple geometry with some parameters given



area ratio  $\frac{A_e}{A_t} = 2$        $\gamma = 1.33$

pressure ratio  $\frac{P_{oe}}{P_{ot}} = 0.98$        $P_{ot} = 30 \text{ psia} = 2.1 \times 10^5 \text{ Pa}$        $P_{atm} = 5 \text{ psia} = 3.4 \times 10^4 \text{ Pa}$   
 $T_{ot} = 2000^\circ R = 1111 \text{ K}$

discharge coefficient  $C_D = 0.98$  (actual mass flow rate/ideal mass flow rate)

mass flow rate  $\dot{m} = 90.7 \text{ kg/s}$

we are also given the mass flow parameter  $MFP = \frac{\dot{m}}{A} \frac{\sqrt{T_o}}{p_o} = M \sqrt{\frac{\gamma}{R} \left( 1 + \frac{\gamma-1}{2} M^2 \right)^{\frac{\gamma+1}{2(\gamma-1)}}$

see Lec. 29

$MFP = 0.5224$  for  $M_t = 1$

# Nozzles

## Example

- starting from the MFP relation, can find the "ideal" throat area

$$MFP = \frac{\dot{m}}{A} \frac{\sqrt{T_o}}{p_o} = M \sqrt{\frac{\gamma}{R} \left( 1 + \frac{\gamma-1}{2} M^2 \right)^{\frac{\gamma+1}{2(\gamma-1)}}}$$

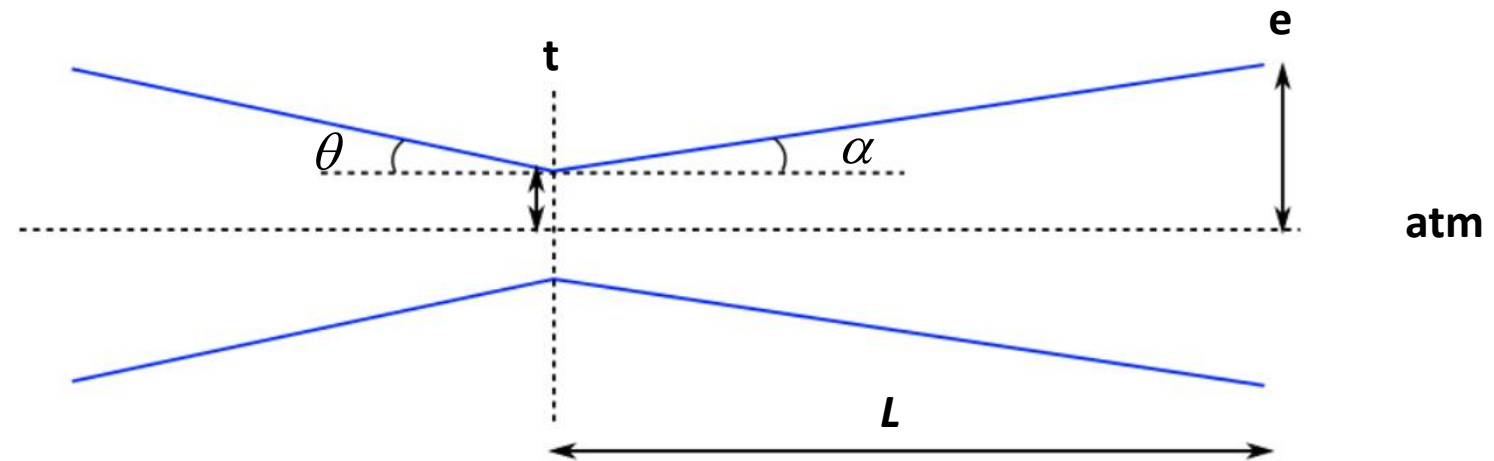
$$\Rightarrow A_{ti} = \frac{\dot{m} \sqrt{T_{ot}}}{p_{ot} MFP(M=1)}$$

- the flow coefficient allows us to determine a "real" throat area  $A_t$

why? actual throat must be sized up slightly to pass the given mass flow rate

$$A_{t,real} = \frac{A_{ti}}{C_D} \Rightarrow \text{assuming circular section, can determine throat radius}$$

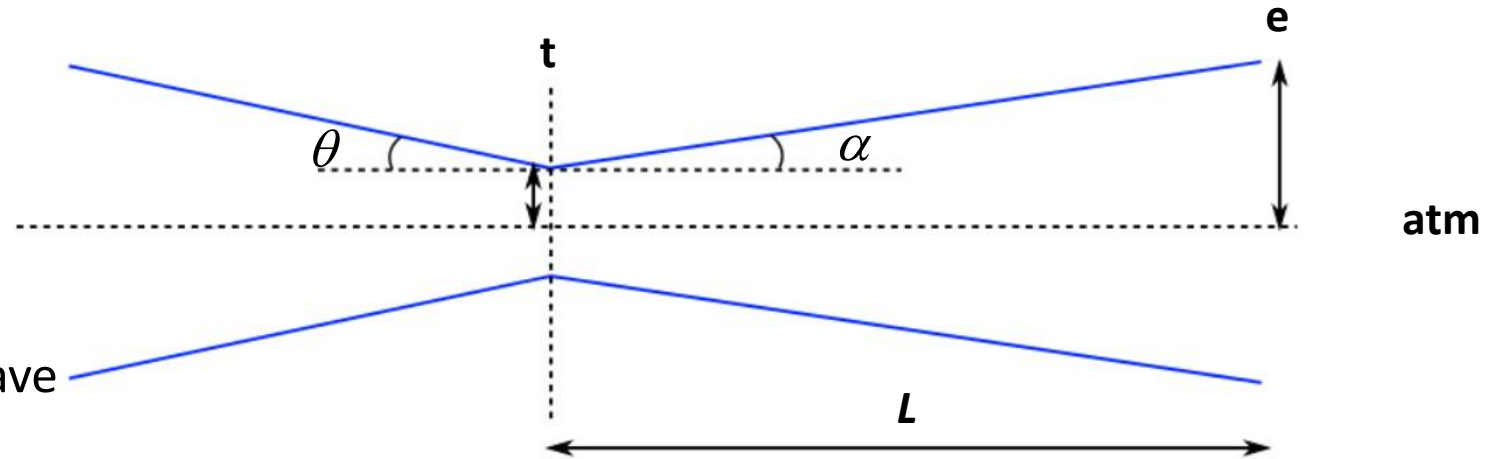
- use given area ratio to determine real area of exhaust  $\frac{A_e}{A_t} = 2$



# Nozzles

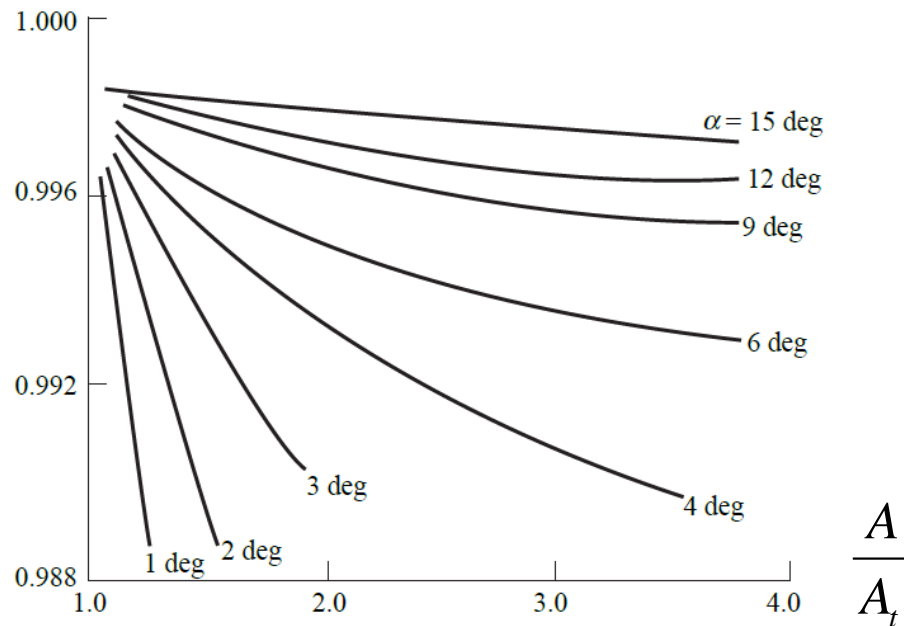
## Example

- we have unknown angles
  - primary nozzle half angle  $\theta$
  - secondary nozzle half angle  $\alpha$
- to determine them, you would generally have reference figures



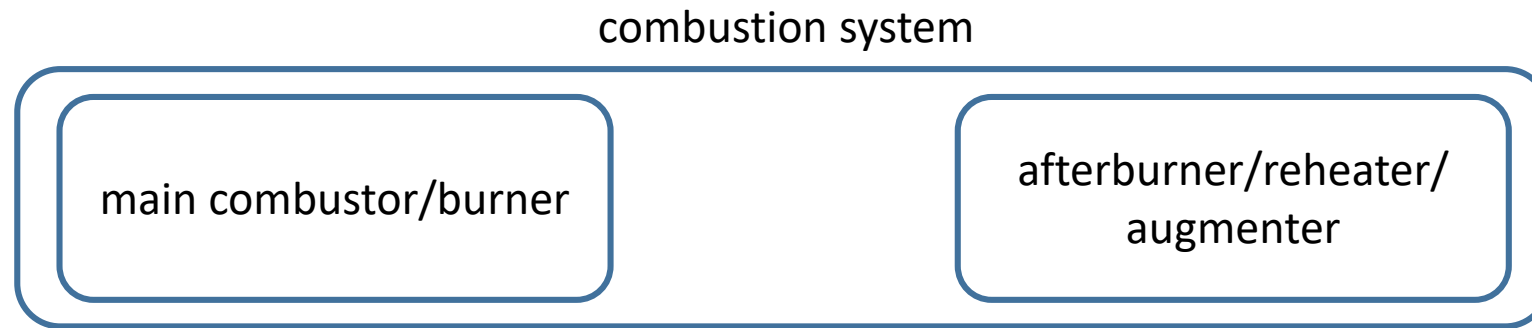
e.g.  $C_V$

would need to determine  $C_V$  and read off corresponding angular value for the area ratio



- from  $\alpha$  and the exhaust area, can determine nozzle length  $L$

## Overview



- aircraft combustion systems differ from conventional devices
  - aircraft: speed up combustion to limit length
  - also higher heat intensities (rate of energy released per unit volume)

turbojet main burner:  $> 1 \times 10^4 \text{ MW/m}^3$

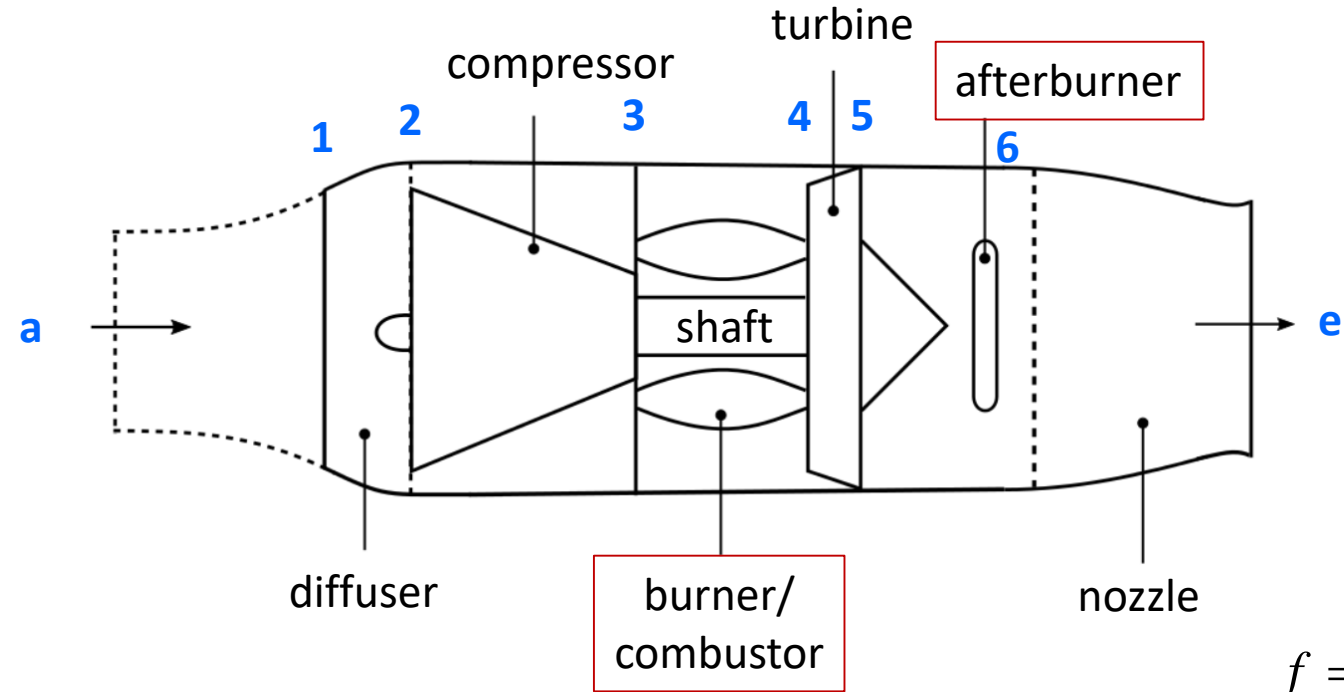
steam power plant:  $\sim 3 \text{ MW/m}^3$

## Characteristics sought

- high combustion efficiency (chemical to thermal)
- low total pressure loss
- combustion stability
- proper temperature distribution at exit with no hot spots (otherwise possible turbine damage)
- short length and small cross section
- no flameout
- long lifetime
- reliable ignition (takeoff, relighting)
- operation over a wide range of mass flow rates, pressures, and temperatures
- low emissions

# Combustors

## Combustor stations in overall system (e.g. turbojet)



- in main combustors: spray fuel into warm air
- simplified combustor energy equation

$$f = \frac{T_{o4} - T_{o3}}{\Delta h_R / c_p - T_{o4}} \quad \text{ideal combustor}$$

see Lec. 13, 14

$$f = \frac{T_{o4}/T_{o3} - 1}{(\eta_b \Delta h_R / c_{pb} T_{o3}) - T_{o4}/T_{o3}} \quad \text{non-ideal combustor}$$

$$\frac{P_{o4}}{P_{o3}} = P_{rb} \quad \text{burner pressure ratio}$$

# Combustors

## Key combustion parameters

### equivalence ratio $\phi$

$$\phi = \frac{f}{f_{stoich}} = \frac{m_{fuel} / m_{ox}}{(m_{fuel} / m_{ox})_{stoich}} = \frac{n_{fuel} / n_{ox}}{(n_{fuel} / n_{ox})_{stoich}}$$

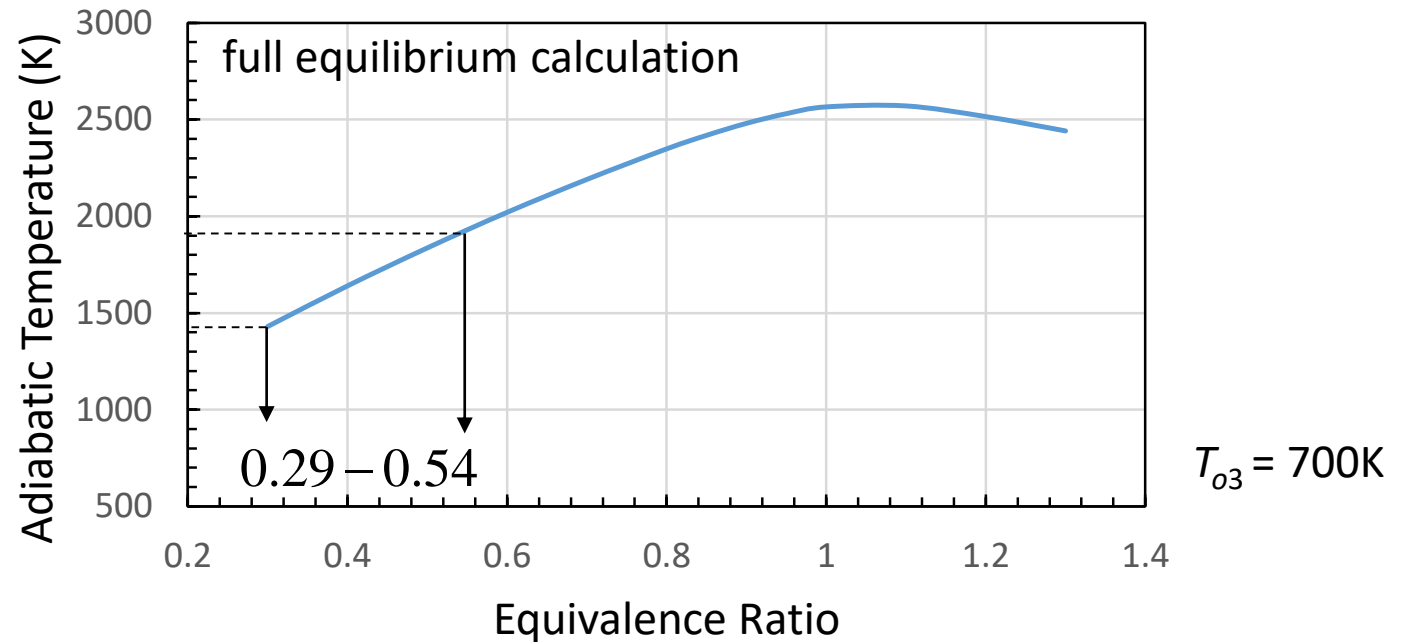
see Lec. 19

$\phi > 1$  : rich fuel – air ratio

$\phi < 1$  : lean fuel – air ratio

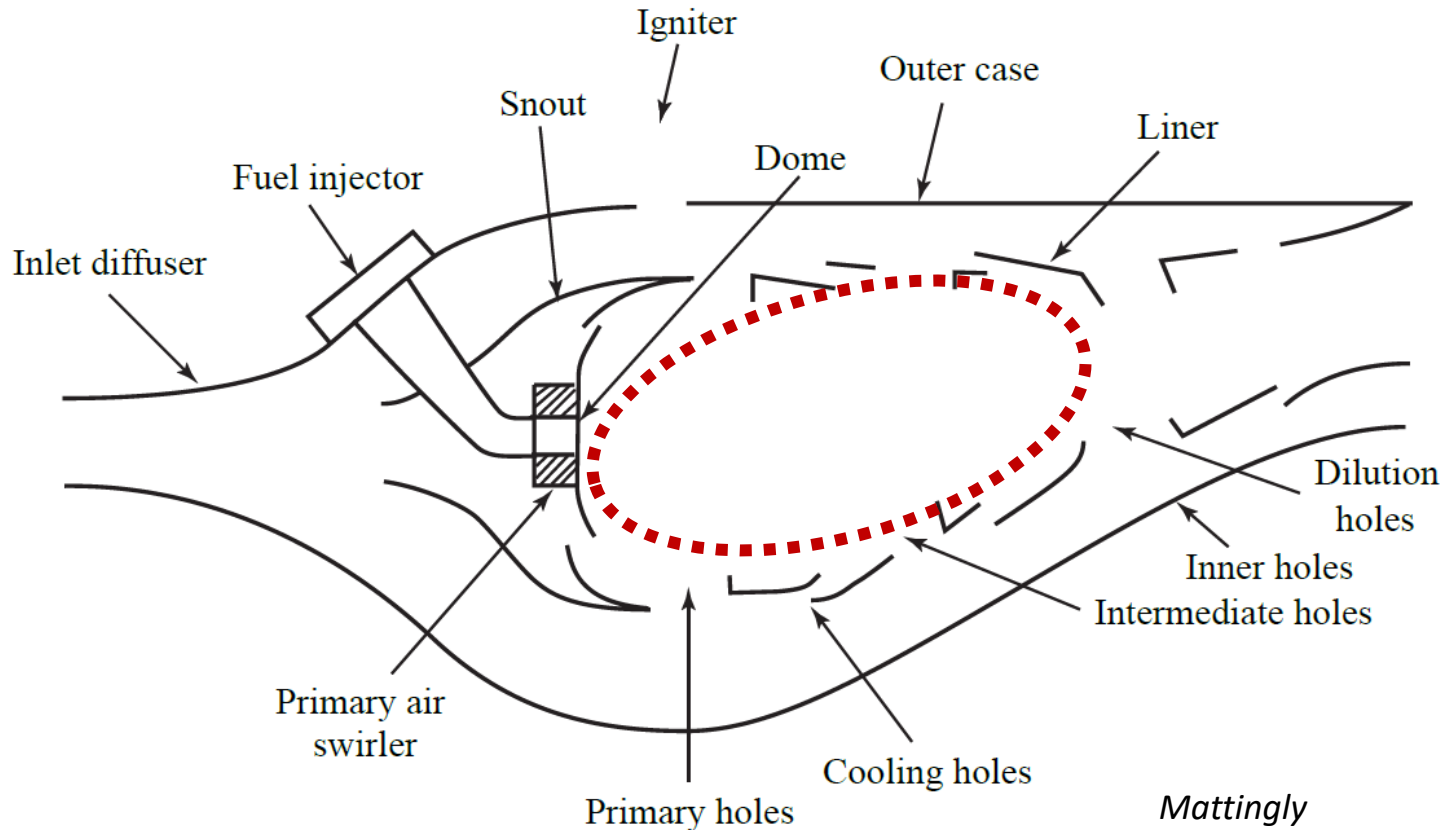
- to prevent excessive temperatures at the exit of main burner or afterburner: use  $\phi < 1$

- value of equivalence ratio: same value regardless of moles (n), mass (m) used
- for jet fuel,  $f_{stoich} \sim 0.067$ ,  $\Delta h_R \sim 43.4$  MJ/kg
- in analyzing combustion reaction, more realistic to consider:
  - non-calorically perfect gas ( $c_p$  varies with T)
  - actual equilibrium composition
- for  $T_{o4,max} = 1400 - 1900$ K, equivalence ratio range limited



# Combustors

## Main combustor components



### 3 principal elements

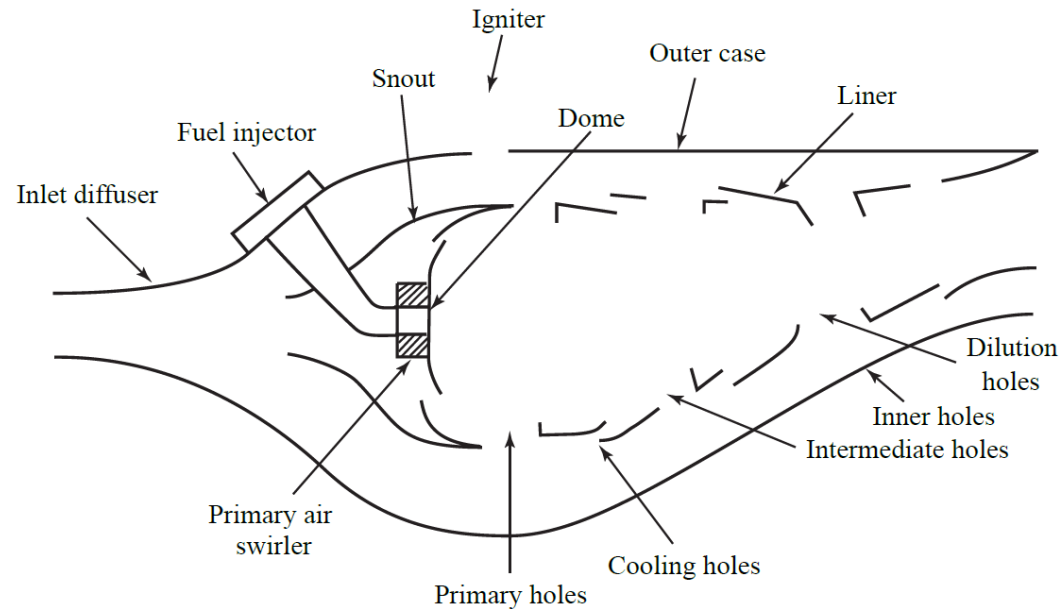
- inlet diffuser
- dome and snout or cowl
- liner

### subcomponents

- fuel injector
- igniter
- burner case
- primary swirler

# Combustors

## Main combustor components



## functions

- **combustor dome**

- produce area of high turbulence and flow shear near fuel nozzle to finely atomize the fuel spray and promote rapid fuel/air mixing

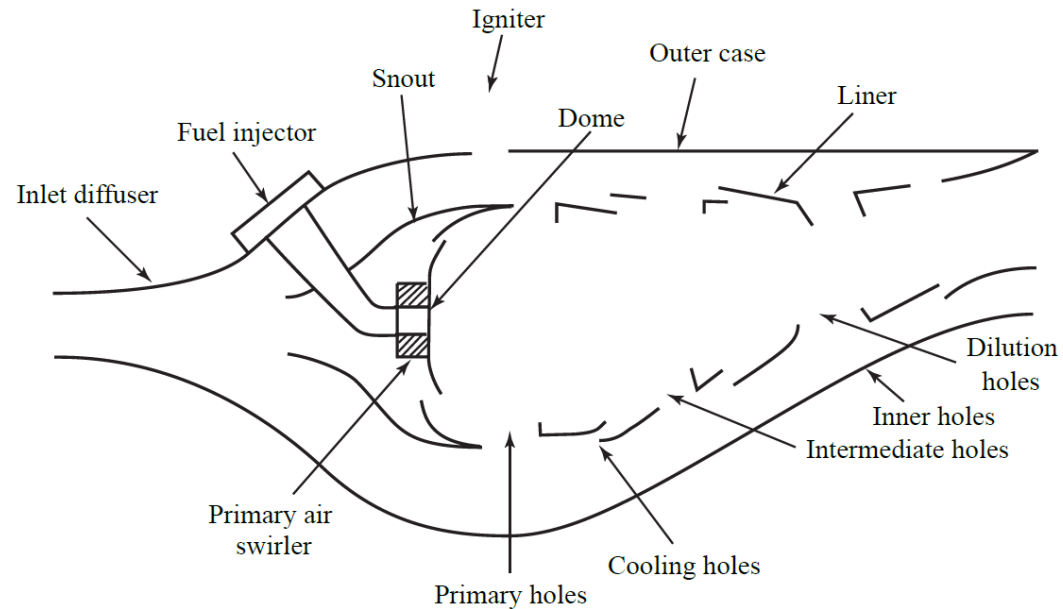
- **inlet diffuser**

- reduce velocity of the air from compressor
- provide air to combustion zone in stable, uniform flowfield
- maximize pressure recovery

- **snout**

- divides incoming air into primary air and other airflows (intermediate, dilution, and cooling air).
- streamlines combustor dome
- permits larger diffuser divergence angle and reduced overall diffuser length

## Main combustor components



## functions

- **liner**

- contains combustion process
- allows introduction of intermediate and dilution airflow and liner's cooling airflow
- must support forces resulting from pressure drop
- must have high thermal resistance capable of continuous and cyclic high-temperature operation
- requires use of high-strength, high-temperature, oxidation-resistant materials (e.g., Hastalloy X) and cooling air

- **injector/atomizer**

- facilitate fuel atomization and mixing

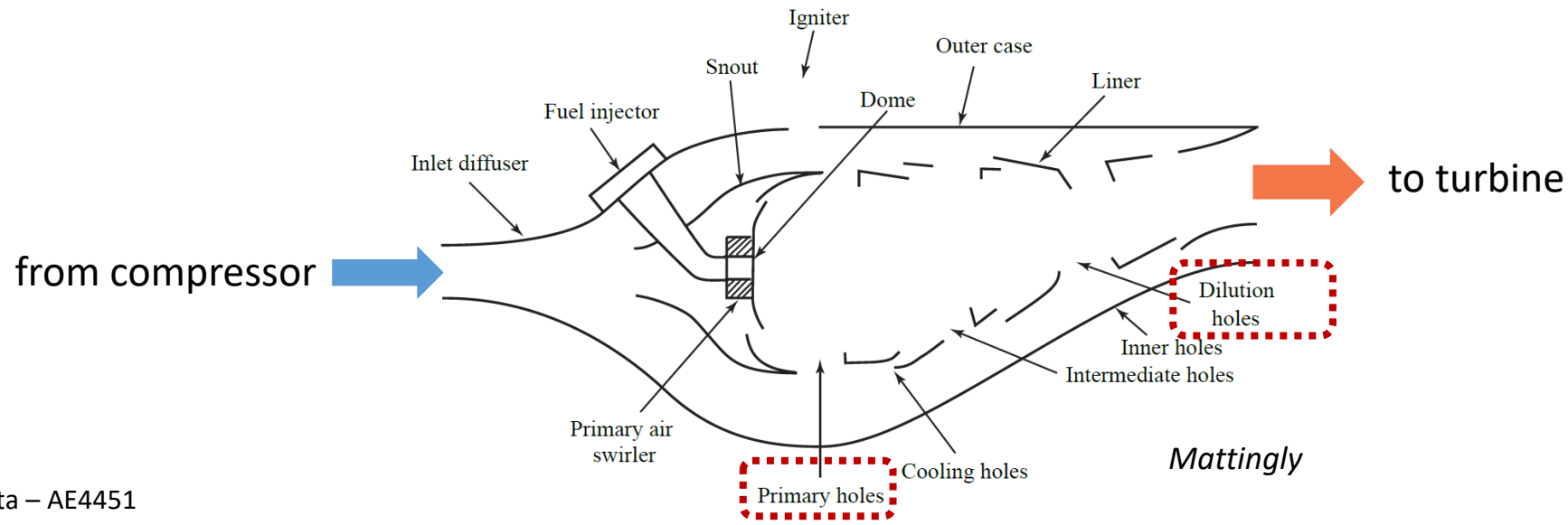
- **igniter**

- spark igniters, similar to automotive spark plugs
- ignites the cold, flowing fuel/air mixture in main burner
- requires 1000s of volts at tip

# Combustors

## Flammability limits and dilution

- for pre-mixed jet fuel-air at typical T3 values, we cannot sustain a flame (without help) below a threshold equivalence ratio value  $\phi$  of 0.35 – 0.43
  - this is the **lean flammability limit**
- for lower range of our operation, we cannot premix all air and fuel entering the combustor
  - run richer in primary zone (more stable)
  - add dilution air downstream (intermediate zone) to lower temperature (known as "**air staging**")
  - also use some of the excess air to cool the combustor walls, keep flame and hot gases away from liner

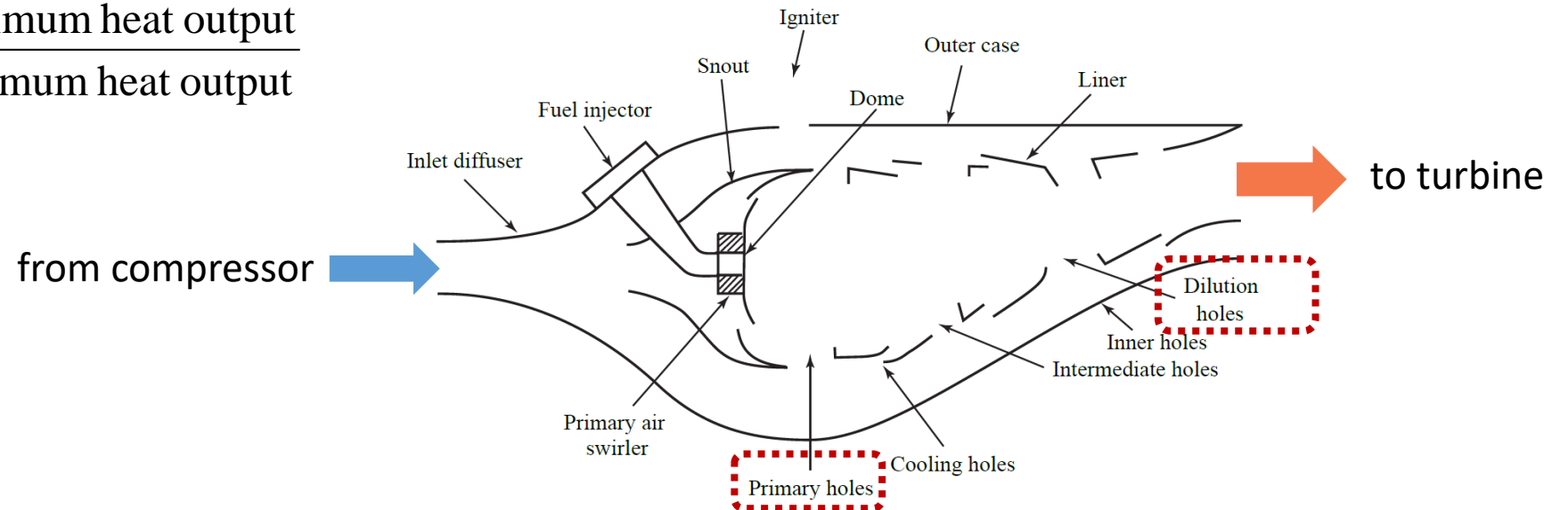


# Combustors

## Air staging options

- to reduce soot and NOx emissions, some combustor designs have moved to increasing the fraction of air introduced near the head end of combustor (lean burn)
- with reduction in dilution air
  - less air for cooling
  - can be harder to reduce hot streaks
  - leaner primary zone susceptible to stability problems
  - can require complicated fuel management for turndown (reduced  $f$ )

turndown ratio of burner:  $\frac{\text{maximum heat output}}{\text{minimum heat output}}$



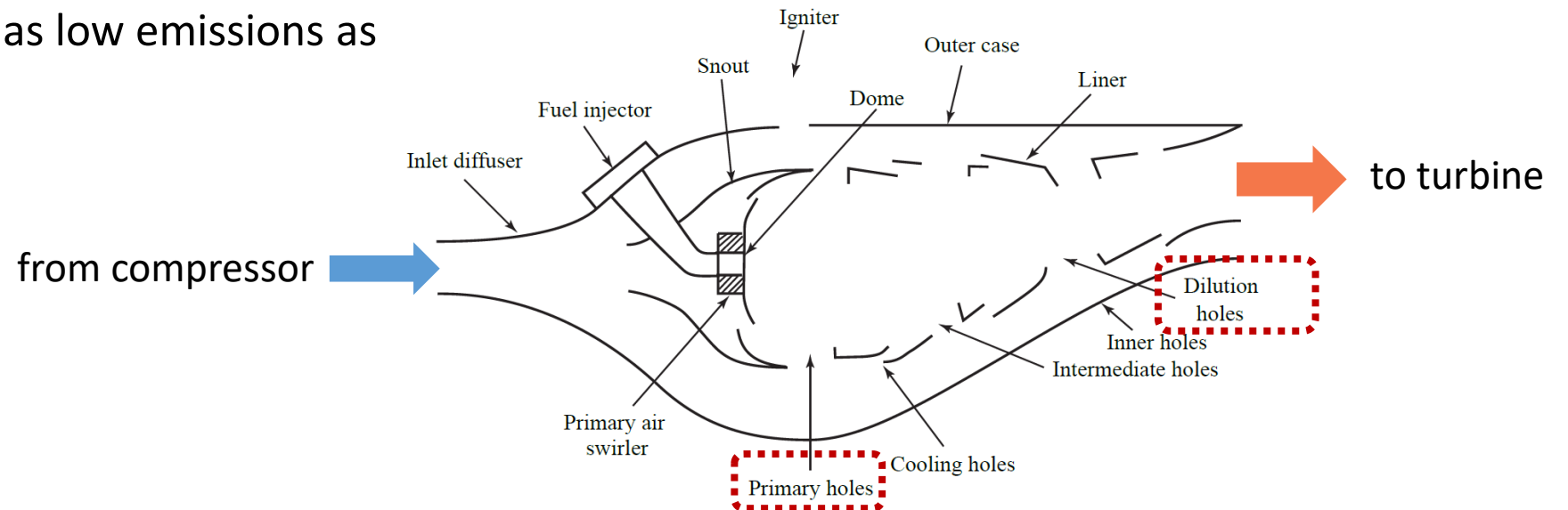
# Combustors

## Air staging options

- alternate approach: maintain original rich primary zone and use strong dilution air jets

referred to as RQL (Rich burn – Quick quench – Lean burn)

- can keep emissions levels low and promote exit uniformity while maintaining stability advantages of rich primary zone
- may not be able to achieve as low emissions as lean burn designs



# Combustors

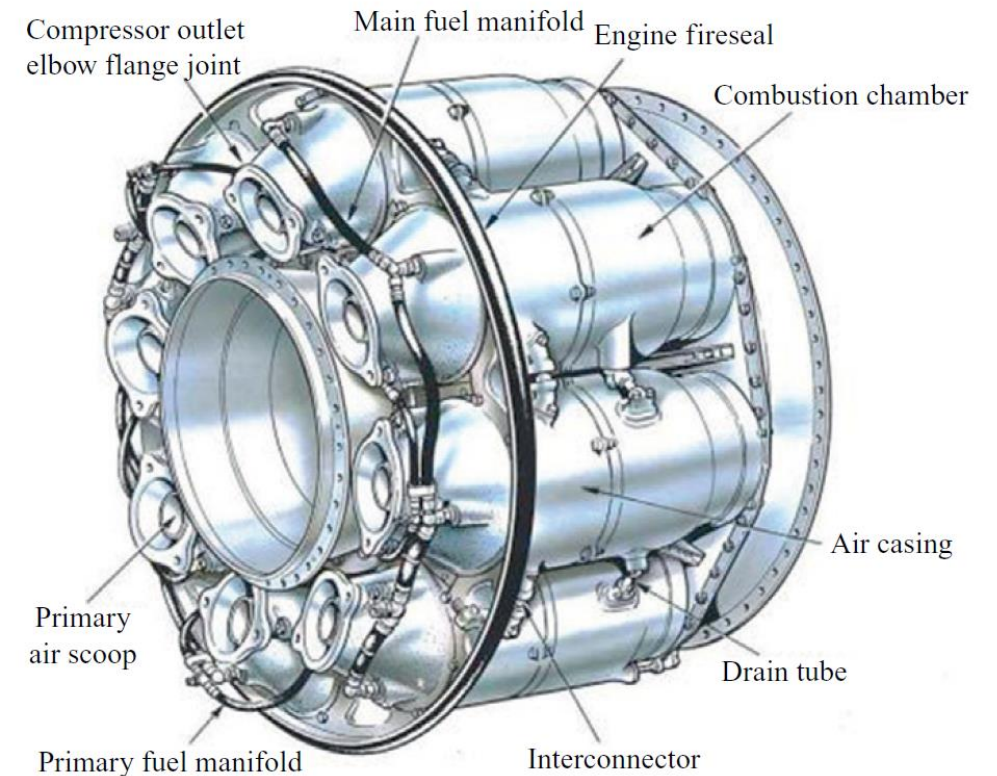
## Main combustor types

3 types

1. can
2. can-annular (cannular)
3. annular

### Can

- one or more cylindrical burners, each contained in a burner case
- each can has fuel injector, liner, interconnectors, casing
- modular design: used during early development of the turbojet engine, facilitates testing
- further advantage: simple control of  $f$
- disadvantage: weight, pressure loss (7%), non-uniformity



*Gharehpetian and Agah, Distributed Generation Systems (2017)*



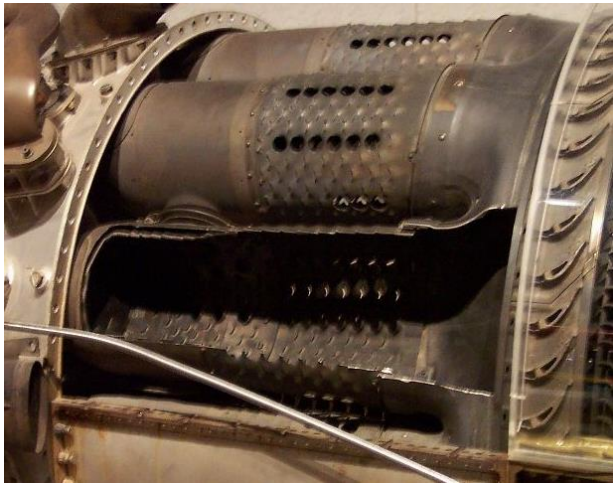
*Jumo004b*

# Combustors

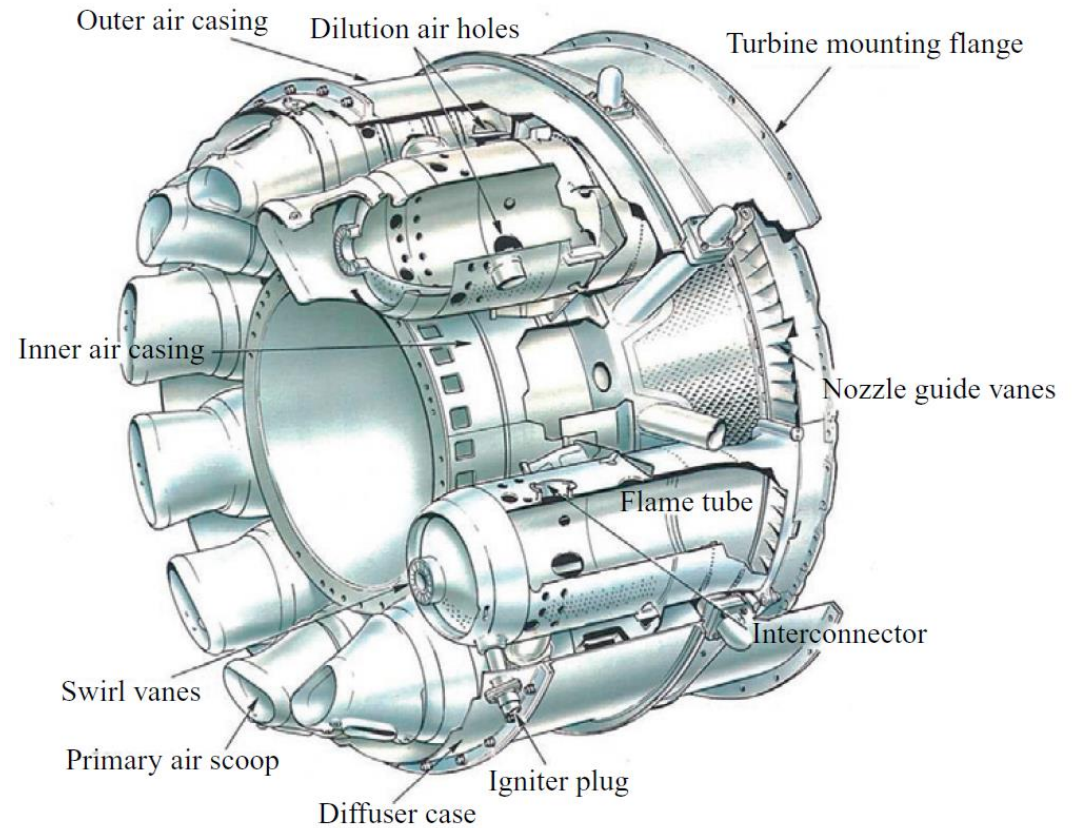
## Main combustor types

### Cannular

- consists of a series of cylindrical burners arranged within a common annulus
- originally most common in the aircraft turbine engines
- slightly lower pressure loss than can configuration (6%)



GE79 combustor (GE Aviation)

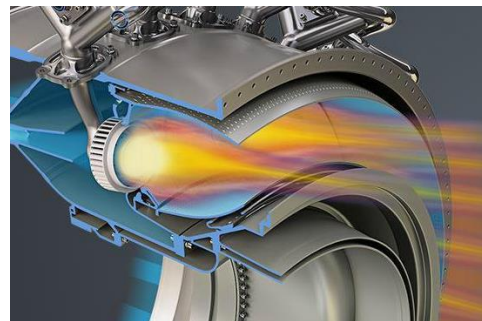


Gharehpetian and Agah, Distributed Generation Systems (2017)

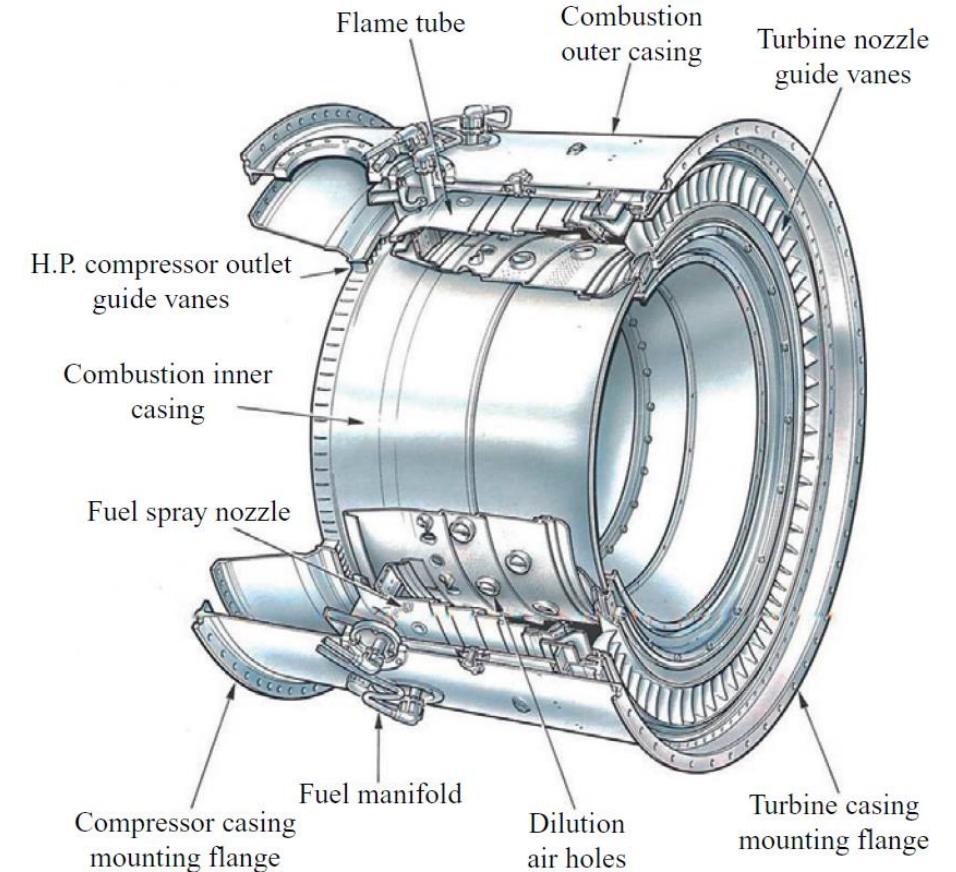
## Main combustor types

### Annular

- consists of a single burner with an annular cross section
- has largely replaced cannular design in modern engines
- multiple favorable features
  - improved combustion zone uniformity
  - design simplicity
  - reduced liner surface area
  - shorter system length
  - minimized pressure loss (5%)
- disadvantage: full rig-testing needed, full liner replacement costly



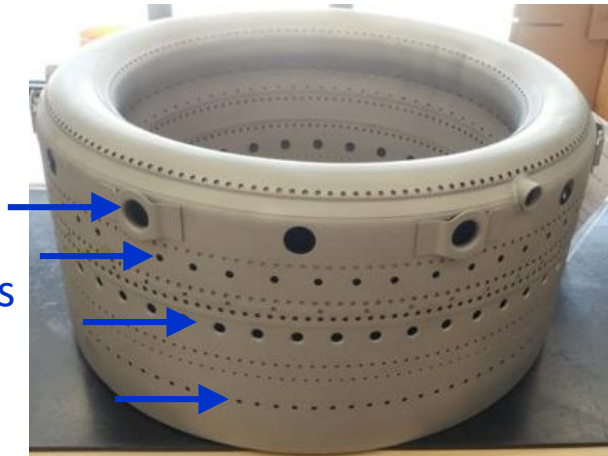
GE90 combustor (GE Aviation)



Gharehpetian and Agah, *Distributed Generation Systems* (2017)

# Combustors

## Annular combustor liners



PT6 (PW Canada, Turboprop, King Air, Cessna)



KJ66 Pegasus (RR, Harrier)



JT9D (PW, 747, 767, A300)

to cool liner:

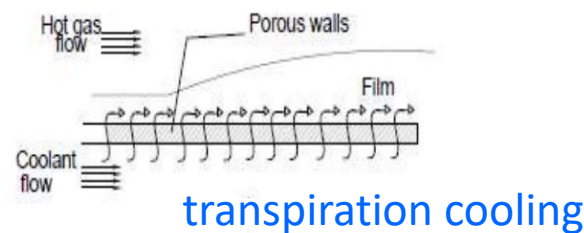
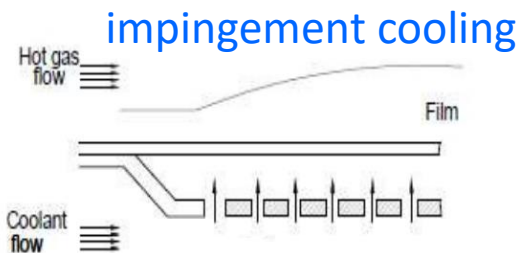
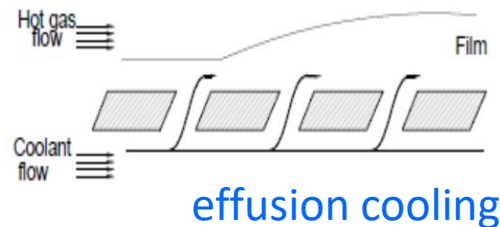
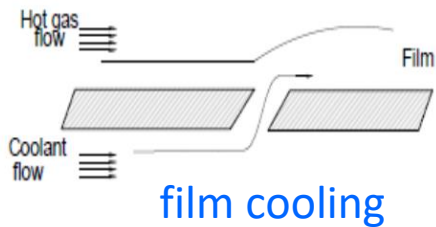
- cooling air flowed between liner and liner outer case
- can define a **cooling effectiveness**

$$\Phi = \frac{T_g - T_m}{T_g - T_c}$$

$T_g$  = mainstream gas temp.

$T_m$  = average metal temp.

$T_c$  = cooling air temp.



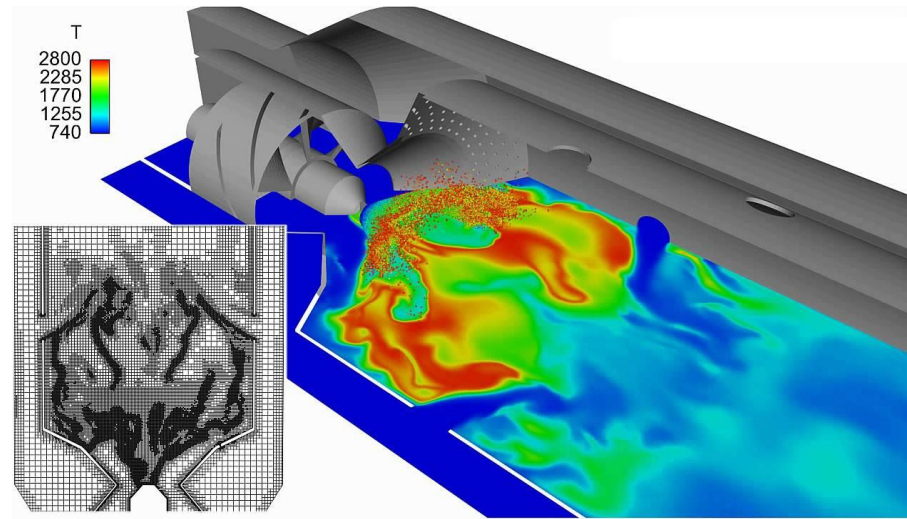
Kumar et al, IOP Conf. Ser.: Mater. Sci. Eng. 804, 012003 (2020)

## Fuel injection/atomization

- liquid hydrocarbon fuels will burn only after becoming a gas/vapor
  - pre-vaporizing fuel in heat exchanger would
    - (i) require additional weight
    - (ii) lead to fuel coking; heated fuel pyrolyzes and forms carbon residue that clogs fuel lines
- combustors therefore use atomizers to produce fine liquid fuel droplets



*3D printed fuel nozzle for LEAP engine (GE)*



*fuel atomization simulation example from convergeCFD*

# Combustors

## Fuel injectors/atomizers

4 types, according to injection method

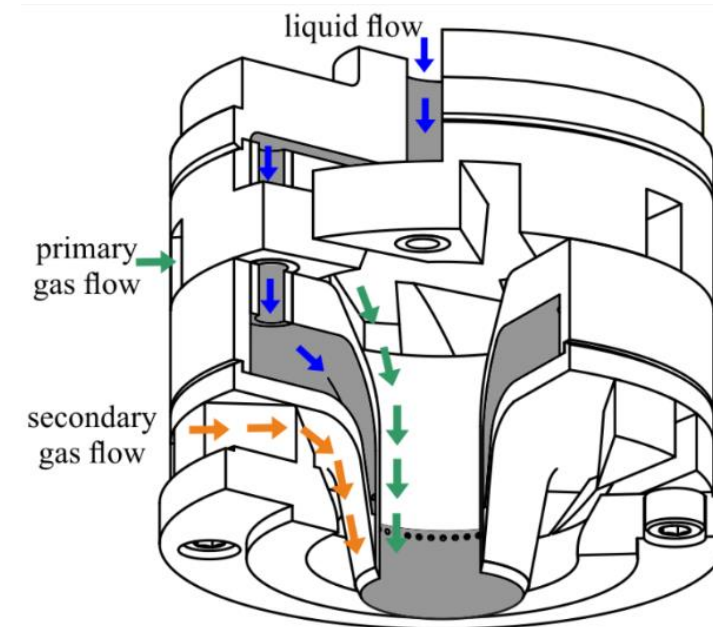
1. pressure-atomizing
2. air blast
3. vaporizing
4. premix/prevaporizing

### Pressure atomizers

- provides best atomization at high pressures; 500 psi above main burner pressure
- poor performance at reduced fuel flow rates (low pressure)
- prone to fuel leaks (due to high fuel pressures) and plugging of orifices from fuel contaminants

### Air blast atomizers

- fuel atomization and mixing through the use of primary air momentum with strong swirling motion
- rely less on fuel pressure and more on shear induced by air flow
- lower fuel pressures: 50 – 200 psi above main burner pressure



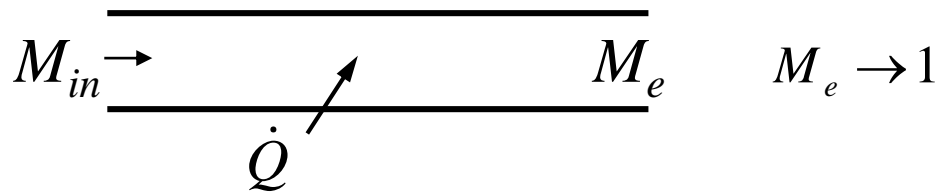
Holz et al., *Energies* 12, 2835 (2019)

# Combustors

## Afterburners/augmentors

- fuel is being injected into high temperature flow
- fuel needs to be distributed radially and azimuthally
- need flame holding for high velocity flow
  - prevents flame from being extinguished
  - creates low speed eddies in the flow
- choking of high speed flow a possibility (heat addition)

### Rayleigh Flow



avoid this by using expanded nozzle area:  
hence variable area nozzle, not simple fixed convergent nozzle

